## Computer-Aided Verification

## Class Quiz (2) Due Date: May 24, 2006

(1) Choose a variable ordering for the set $\{a, b, c, d\}$ and draw the BDD for the expression

$$
(a \wedge b \wedge c) \vee(\neg b \wedge d) \vee(\neg c \wedge d)
$$

Try to find an ordering that is optimal for reducing the BDD size.
(2) Given two dense clock variables x and y , construct a canonical DBM for the following clock zones.
(a) $(x-y \geq 10) \wedge(x \leq 5) \wedge(y \geq 2)$
(b) $(y-x<5) \wedge(x>15) \wedge(y<2)$
(c) $(x<6) \wedge(y>12)$
(3) For the clock zone 2(a) in the above problem, compute the successor clock zone when a transition is taken. The transition has trigger $\mathrm{x}=3$ and clock y is reset.
(4) Given 2 clocks $x$ and $y$, such that the maximum constants compared with $x$ and $y$ are, respectively, 2 and 3 , compute the number of clock regions.
(5) Express the following CTL formula using fixpoint notations.
(a) $A(p \cup E F q)$
(b) $\mathrm{E}(\mathrm{r} \rightarrow \mathrm{AXt})$
(c) $\mathrm{A}(\mathrm{p} \wedge \mathrm{EGq})$
(d) EGAG f
(e) AGEF f

