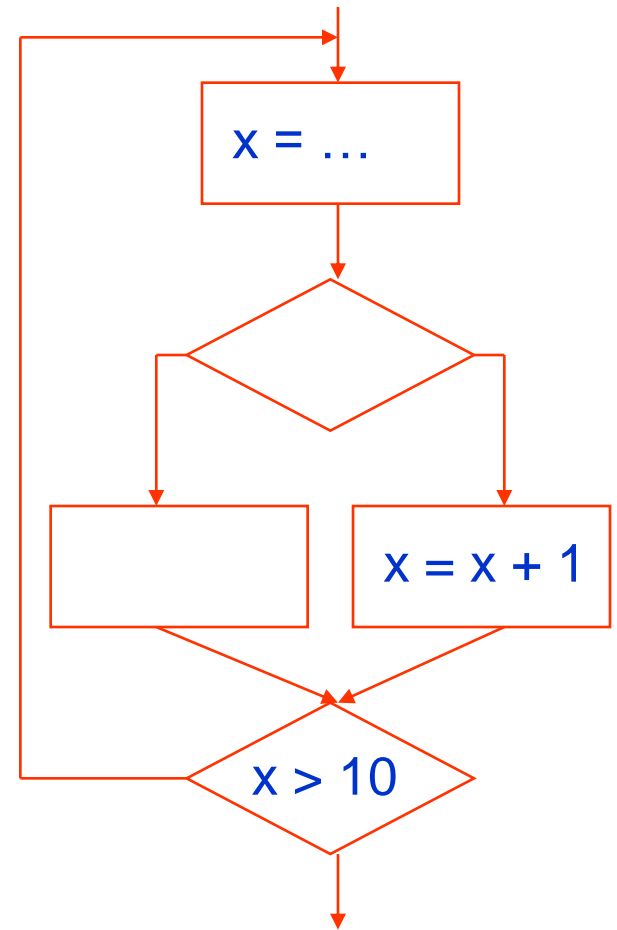

Data Flow Testing

Data Flow Testing

- **Data flow testing** uses the control flow graph to explore the unreasonable things that can happen to data (data flow anomalies).
 - **Data flow anomalies** are detected based on the associations between values and variables.
 - Variables are used without being initialized.
 - Initialized variables are not used once.
-

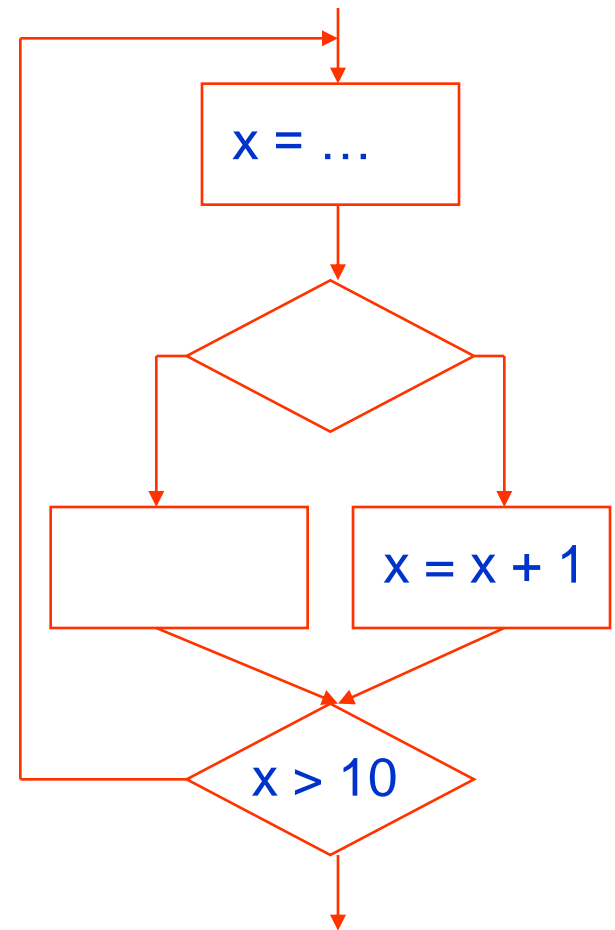
Definitions and Uses of Variables

- An occurrence of a variable in the program is a **definition** of the variable if a value is bound to the variable at that occurrence.
- An occurrence of a variable in the program is a **use** of the variable if the value of the variable is referred at that occurrence.



Predicate Uses and Computation Uses

- A use of a variable is a **predicate use (p-use)** if the variable is in a predicate and its value is used to decide an execution path.
- A use of a variable is a **computation use (c-use)** if the value of the variable is used to compute a value for defining another variable or as an output value.

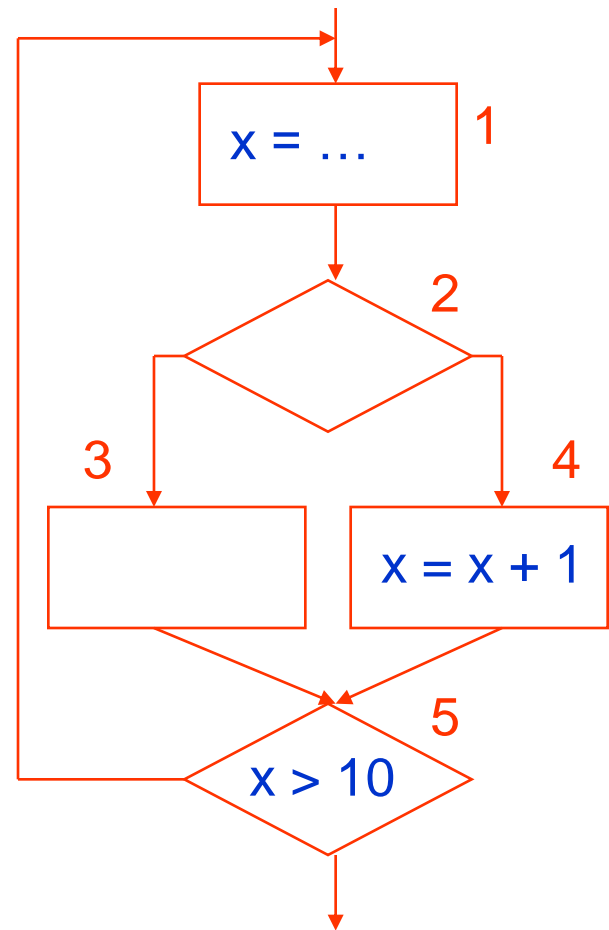


Definition Clear Paths

- A path $(i, n_1, n_2, \dots, n_m, j)$ is a **definition-clear path** for a variable x from i to j if n_1 through n_m do not contain a definition of x .

(1, 2, 4)

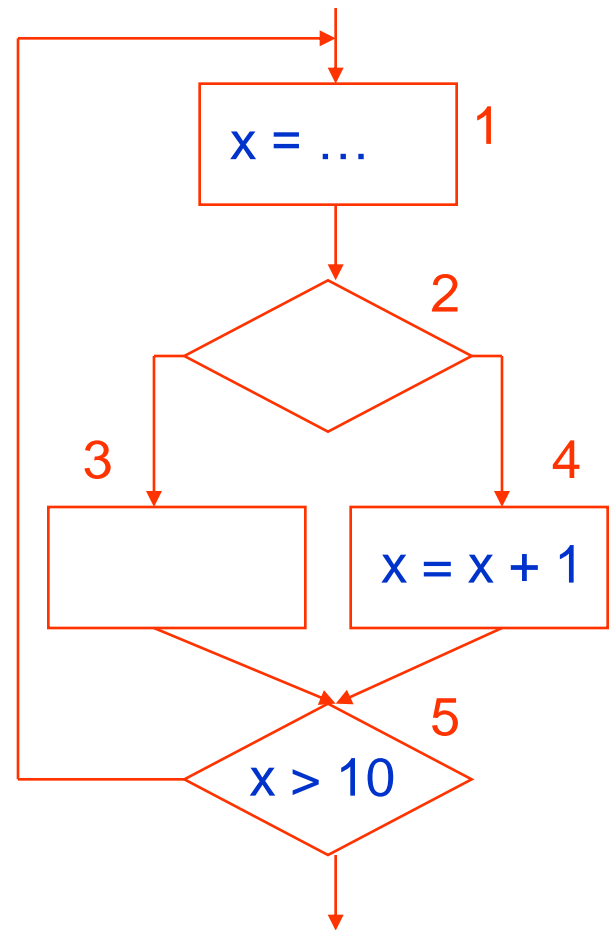
(1, 2, 3, 5)



Definition-C-Use Associations

- Given a definition of x in node n_d and a c-use of x in node n_{c-use} , the presence of a definition-clear path for x from n_d to n_{c-use} establishes the **definition-c-use association** (n_d, n_{c-use}, x) .

$(1, 4, x)$

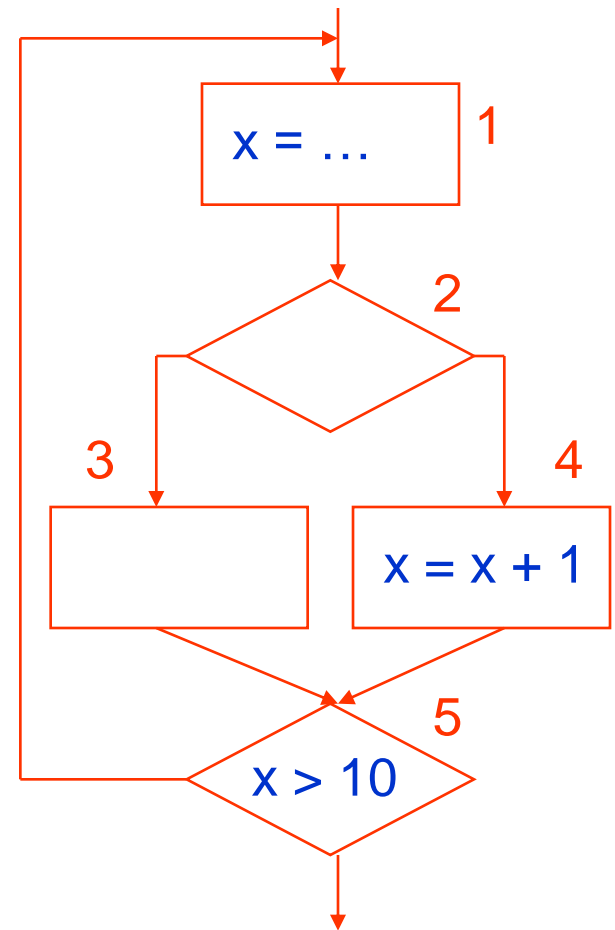


Definition-P-Use Associations

- Given a definition of x in node n_d and a p-use of x in node n_{p-use} , the presence of a definition-clear path for x from n_d to n_{p-use} establishes a pair of **definition-p-use associations** $(n_d, (n_{p-use}, t), x)$ and $(n_d, (n_{p-use}, f), x)$.

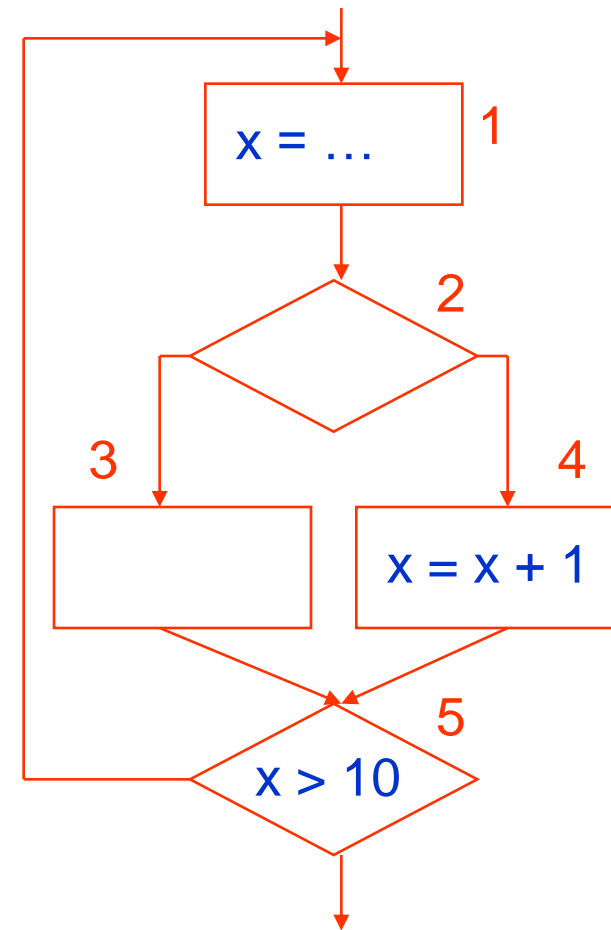
$(1, (5, t), x)$

$(1, (5, f), x)$



DU-Paths

- A path (n_1, \dots, n_m) is a **du-path** for variable x if n_1 contains a definition of x and either n_m has a c-use of x and (n_1, \dots, n_m) is a **definition-clear simple path** for x (all nodes, except possibly n_1 and n_m , are distinct) or is a p-use of x and is a **definition-clear loop-free path** for x (all nodes are distinct) .



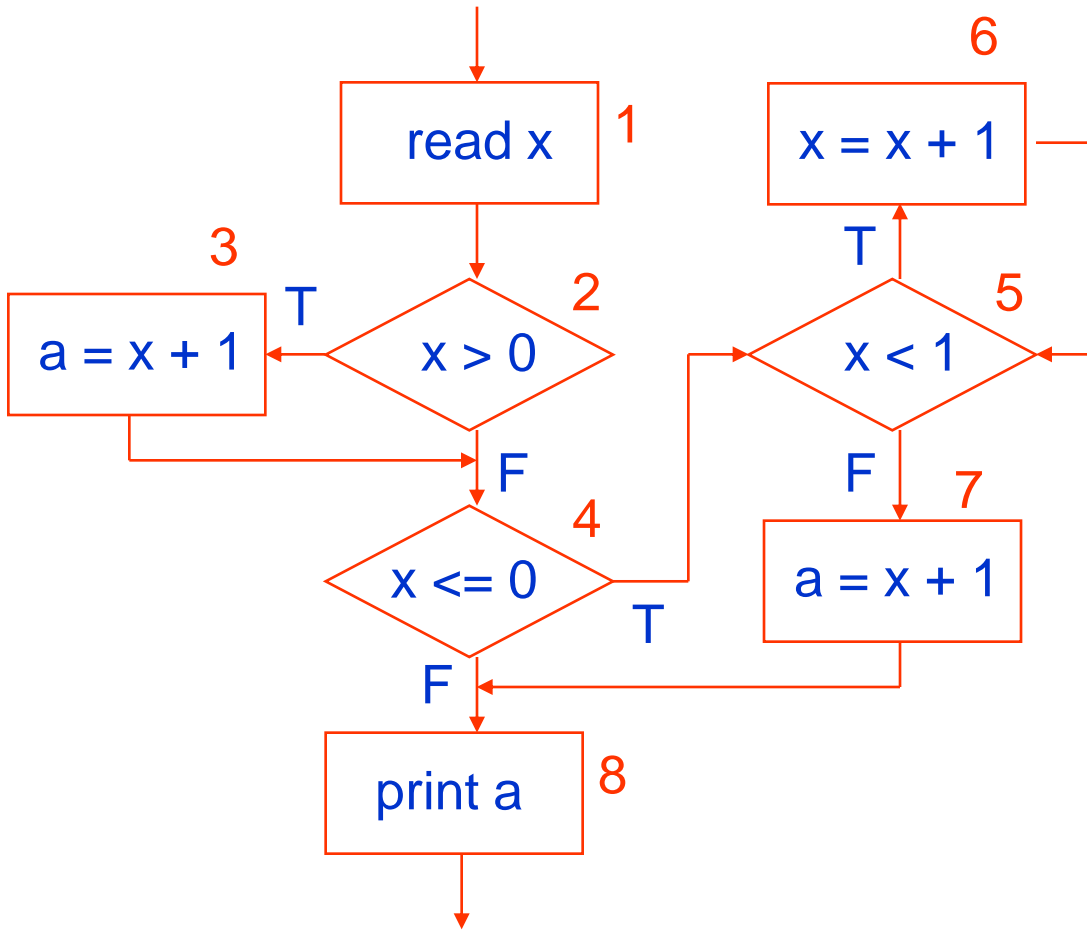
(1, 2, 4)

(1, 2, 3, 5)

Test Coverage Criteria

- All-defs coverage
 - All-c-uses coverage
 - All-c-uses/some-p-uses coverage
 - All-p-uses coverage
 - All-p-uses/some-c-uses coverage
 - All-uses coverage
 - All-du-paths coverage
-

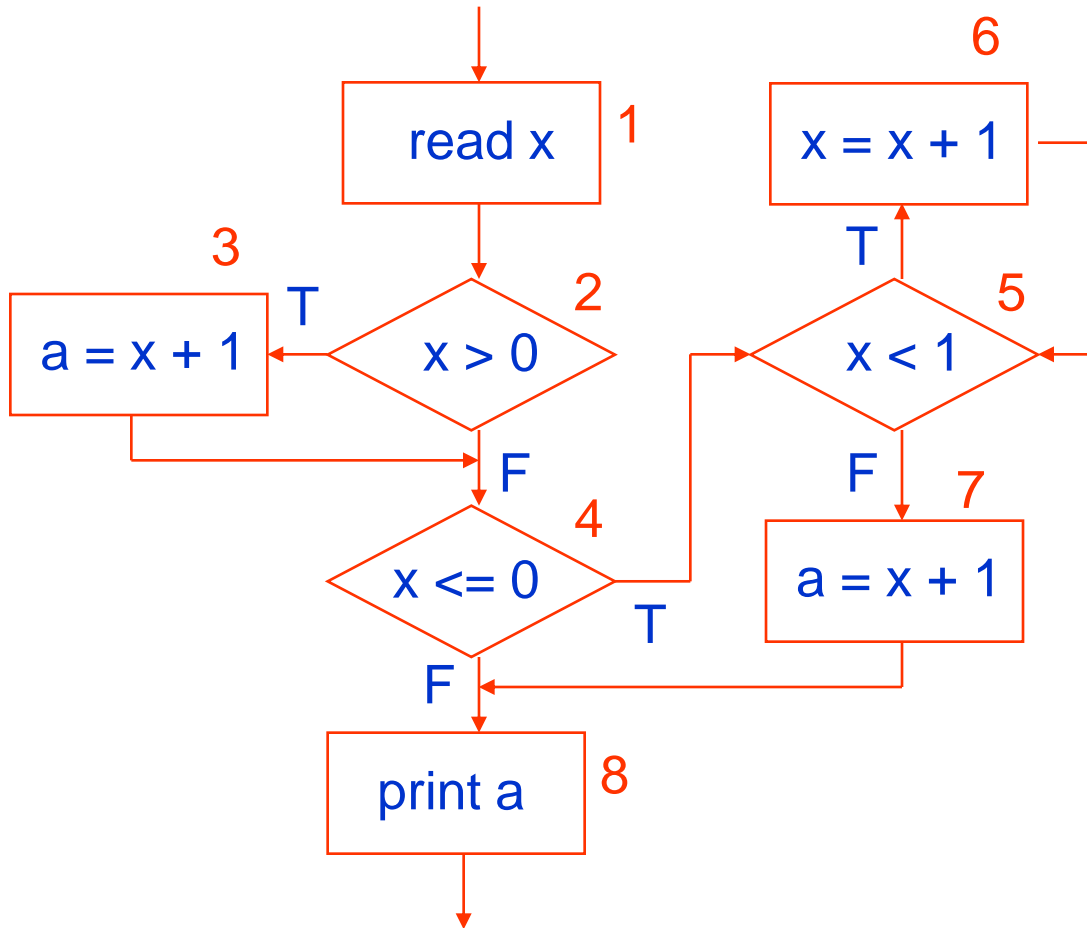
A Running Example



$x = 1$
 $P_1: (1, 2, 3, 4, 8)$
 $a = 2$

$x = -1$
 $P_2: (1, 2, 4, 5, 6,$
 $5, 6, 5, 7, 8)$
 $a = 2$

A Running Example



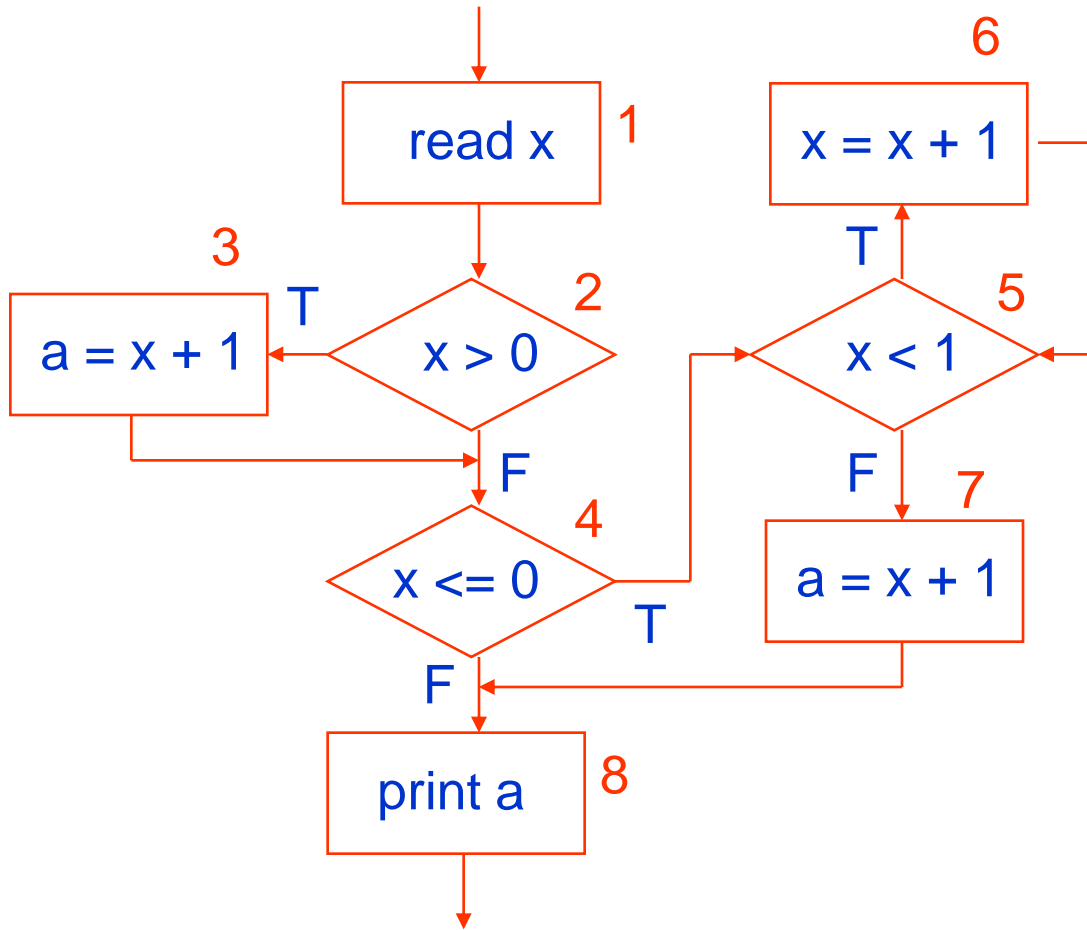
Associations:

- (1, (2, t), x)
- (1, (2, f), x)
- (1, 3, x)
- (1, (4, t), x)
- (1, (4, f), x)
- (1, (5, t), x)
- (1, (5, f), x)
- (1, 6, x)
- (1, 7, x)
- (3, 8, a)
- (6, 6, x)
- (6, 7, x)
- (6, (5, t), x)
- (6, (5, f), x)
- (7, 8, a)

All-Defs Coverage

- Test cases include a definition-clear path from every definition to some corresponding use (c-use or p-use).

All-Defs Coverage

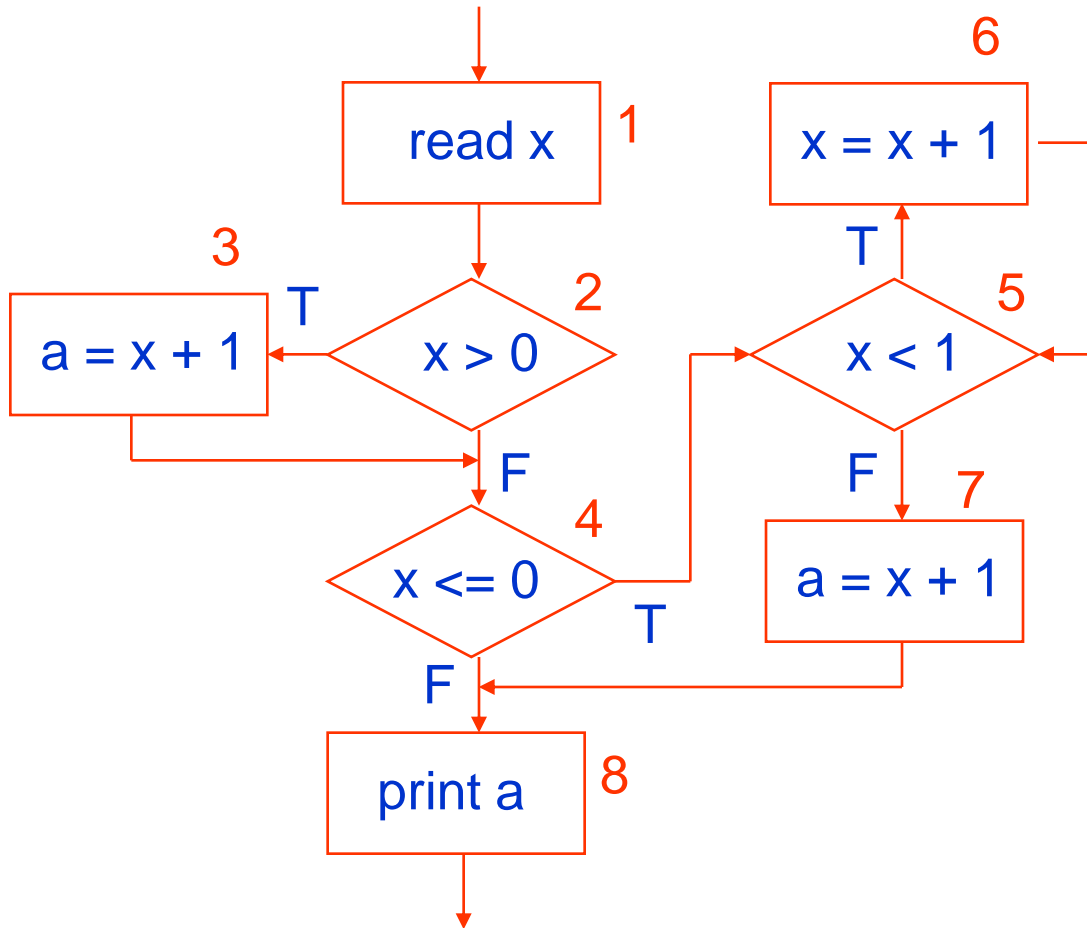


Associations	all-defs
(1, (2, t), x)	✓
(1, (2, f), x)	
(1, 3, x)	
(1, (4, t), x)	
(1, (4, f), x)	
(1, (5, t), x)	
(1, (5, f), x)	
(1, 6, x)	
(1, 7, x)	
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	
(6, (5, t), x)	
(6, (5, f), x)	
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

All-C-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding c-uses.

All-C-Uses Coverage



Associations all-c-uses

(1, (2, t), x)

(1, (2, f), x)

(1, 3, x)

✓

(1, (4, t), x)

(1, (4, f), x)

(1, (5, t), x)

(1, (5, f), x)

(1, 6, x)

✓

(1, 7, x)

✓

(3, 8, a)

✓

(6, 6, x)

✓

(6, 7, x)

✓

(6, (5, t), x)

(6, (5, f), x)

(7, 8, a)

✓

Paths

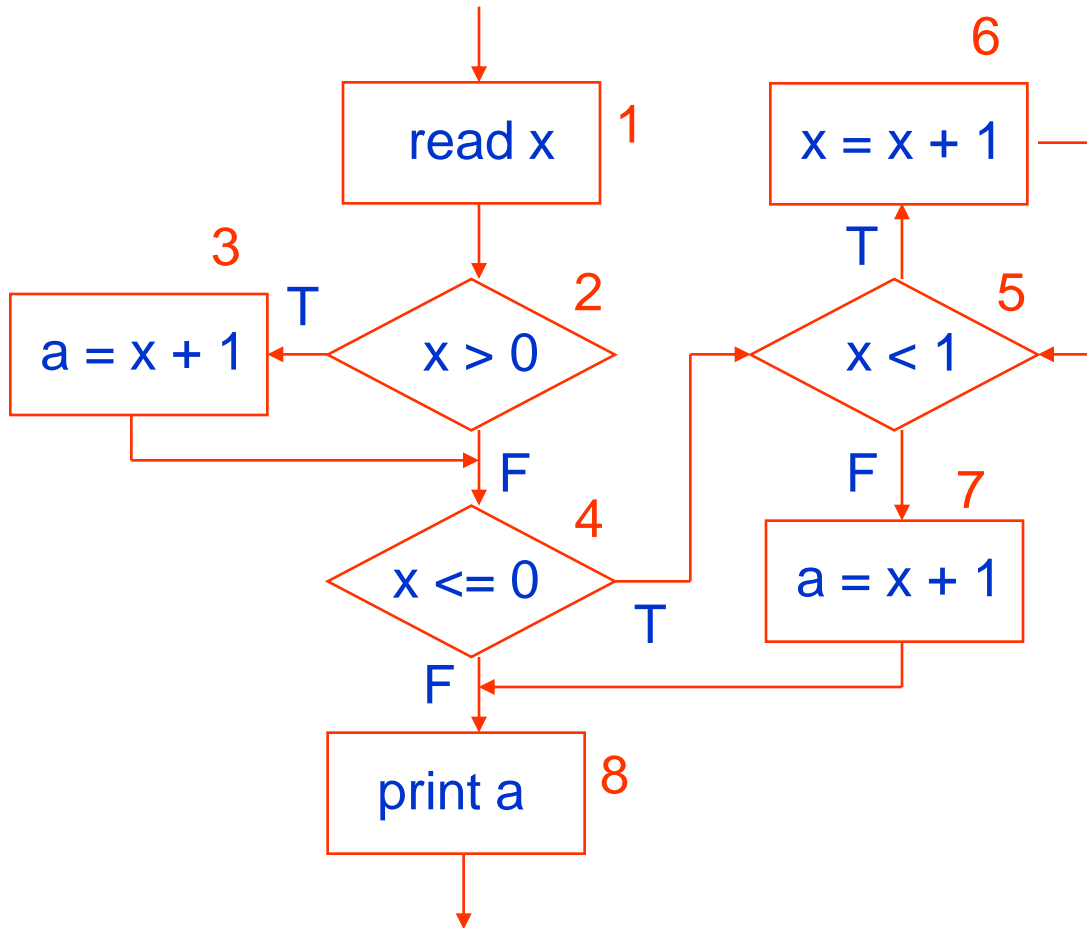
{P₁, P₂}

All-P-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding p-uses.



All-P-Uses Coverage

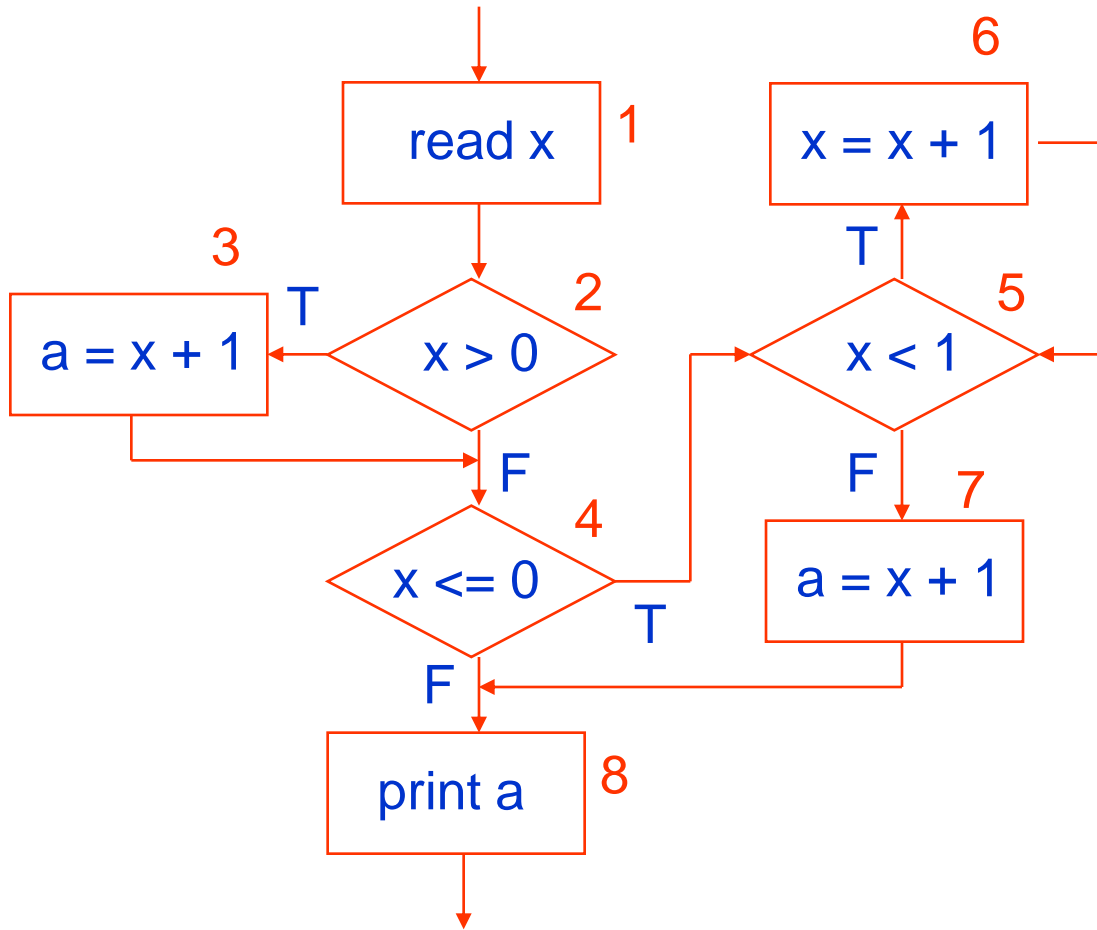


Associations	all-p-uses
(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	
(1, 7, x)	
(3, 8, a)	
(6, 6, x)	
(6, 7, x)	
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	
Paths	{P ₁ , P ₂ }

All-C-Uses/Some-P-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding c-uses. In addition, if a definition has no c-use, then test cases include a definition-clear path to some p-use.
-

All-C-Uses/Some-P-Uses Coverage



Associations all-c-uses/
some-p-uses

(1, (2, t), x)

(1, (2, f), x)

(1, 3, x)

(1, (4, t), x)

(1, (4, f), x)

(1, (5, t), x)

(1, (5, f), x)

(1, 6, x)

(1, 7, x)

(3, 8, a)

(6, 6, x)

(6, 7, x)

(6, (5, t), x)

(6, (5, f), x)

(7, 8, a)

Paths

{P₁, P₂}

✓

✓

✓

✓

✓

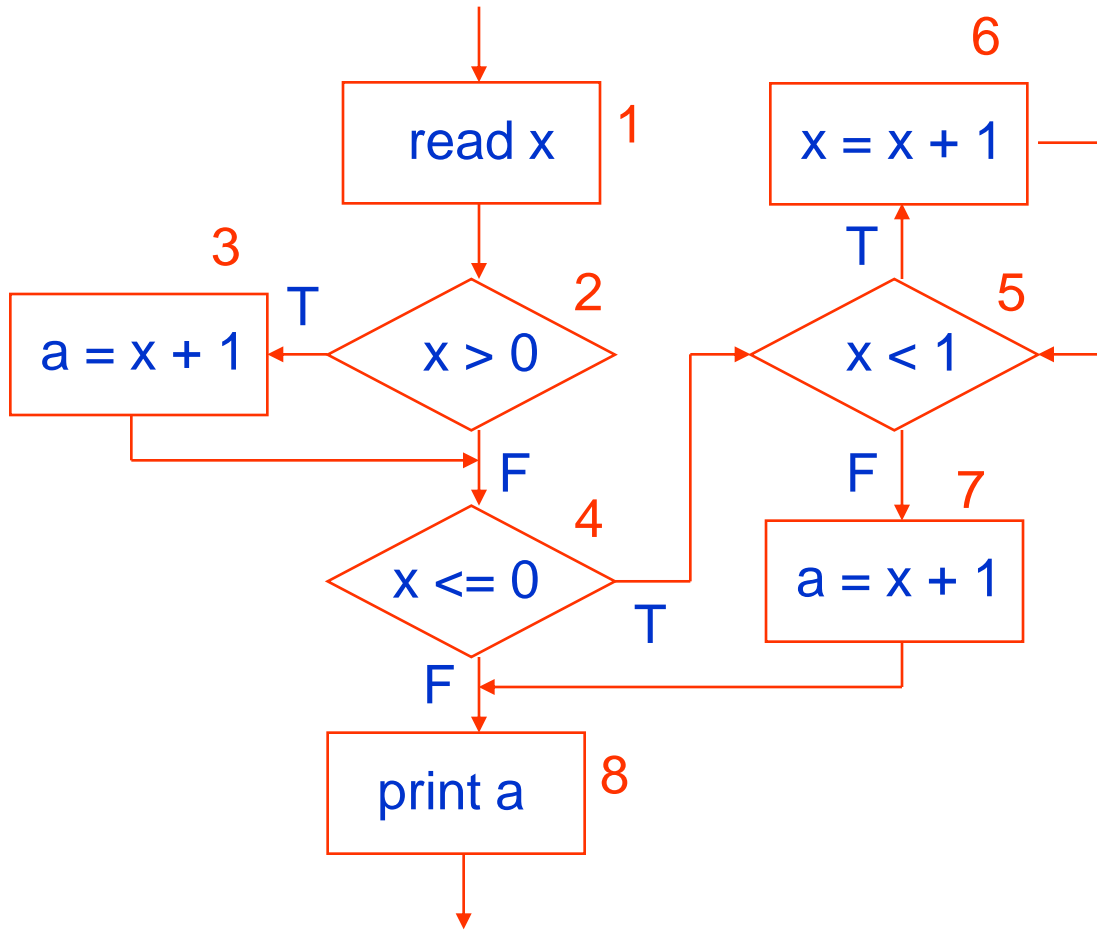
✓

✓

All-P-Uses/Some-C-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding p-uses. In addition, if a definition has no p-use, then test cases include a definition-clear path to some c-use.
-

All-P-Uses/Some-C-Uses Coverage



Associations all-p-uses/
some-c-uses

(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	
(1, 7, x)	
(3, 8, a)	✓
(6, 6, x)	
(6, 7, x)	
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓

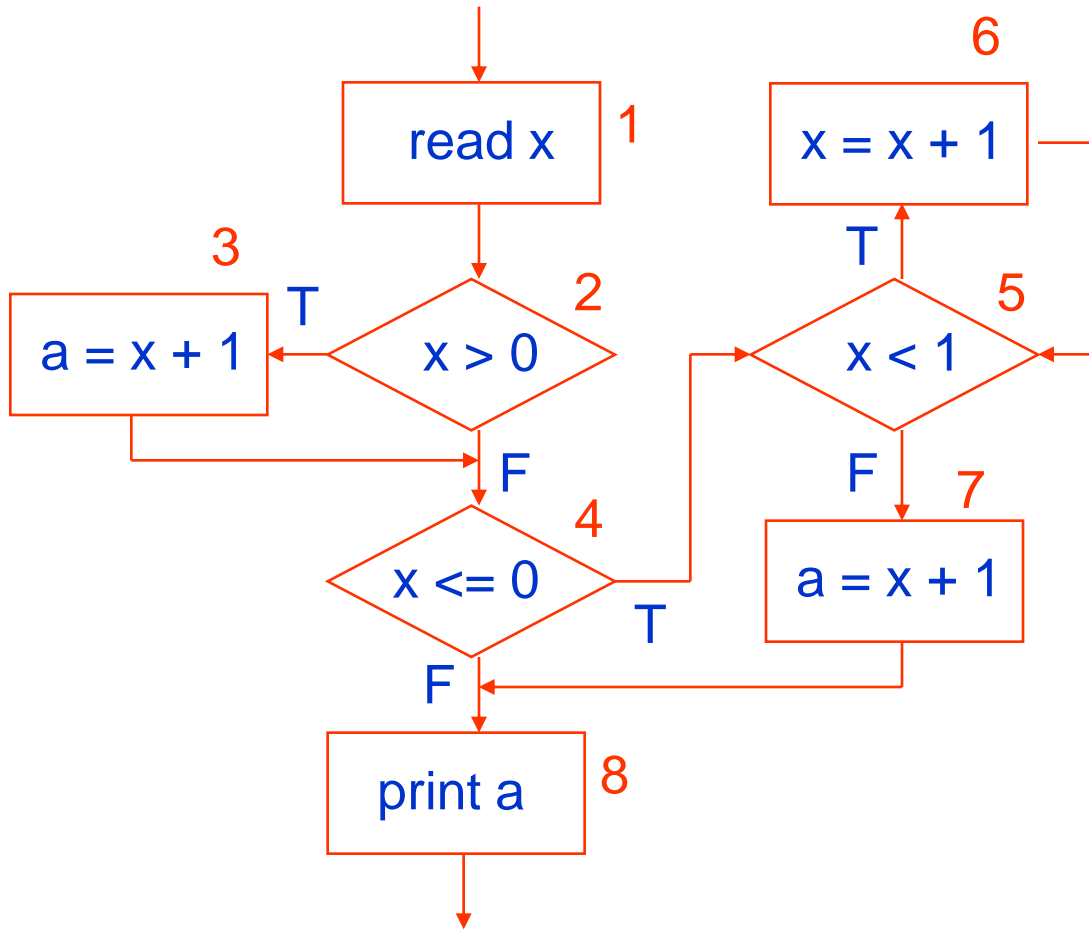
Paths

{P₁, P₂}

All-Uses Coverage

- Test cases include a definition-clear path from every definition to each of its uses including both c-uses and p-uses.
-

All-Uses Coverage

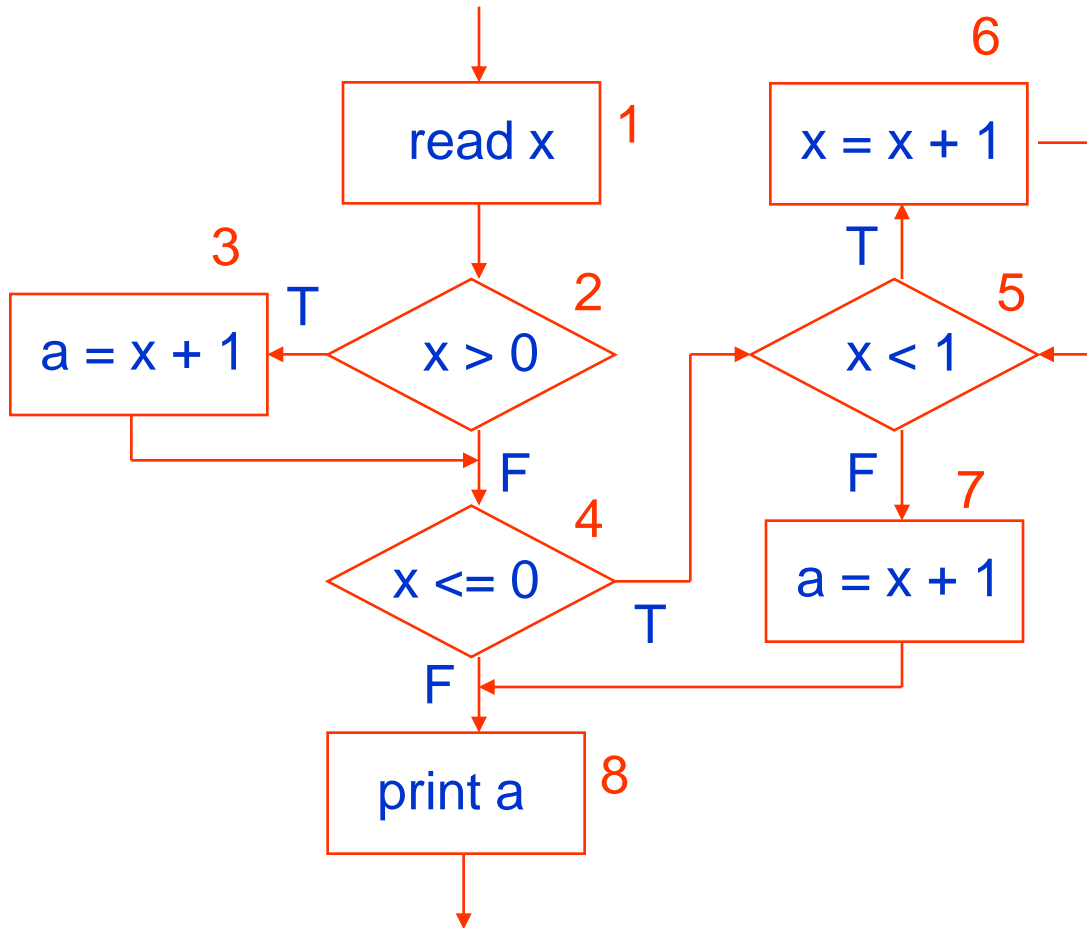


Associations	all-uses
(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	✓
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	✓
(1, 7, x)	✓
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	✓
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

All-DU-Paths Coverage

- Test cases include all du-paths for each definition. Therefore, if there are **multiple paths** between a given definition and a use, they must all be included.
-

All-DU-Paths Coverage



Associations	all-du-paths
(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	✓
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	✓
(1, 7, x)	✓
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	✓
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

Test Coverage Criteria Hierarchy

all-paths



all-du-paths



all-uses



all-c-uses/some-p-uses

all-p-uses/some-c-uses



all-c-uses



all-defs



all-p-uses

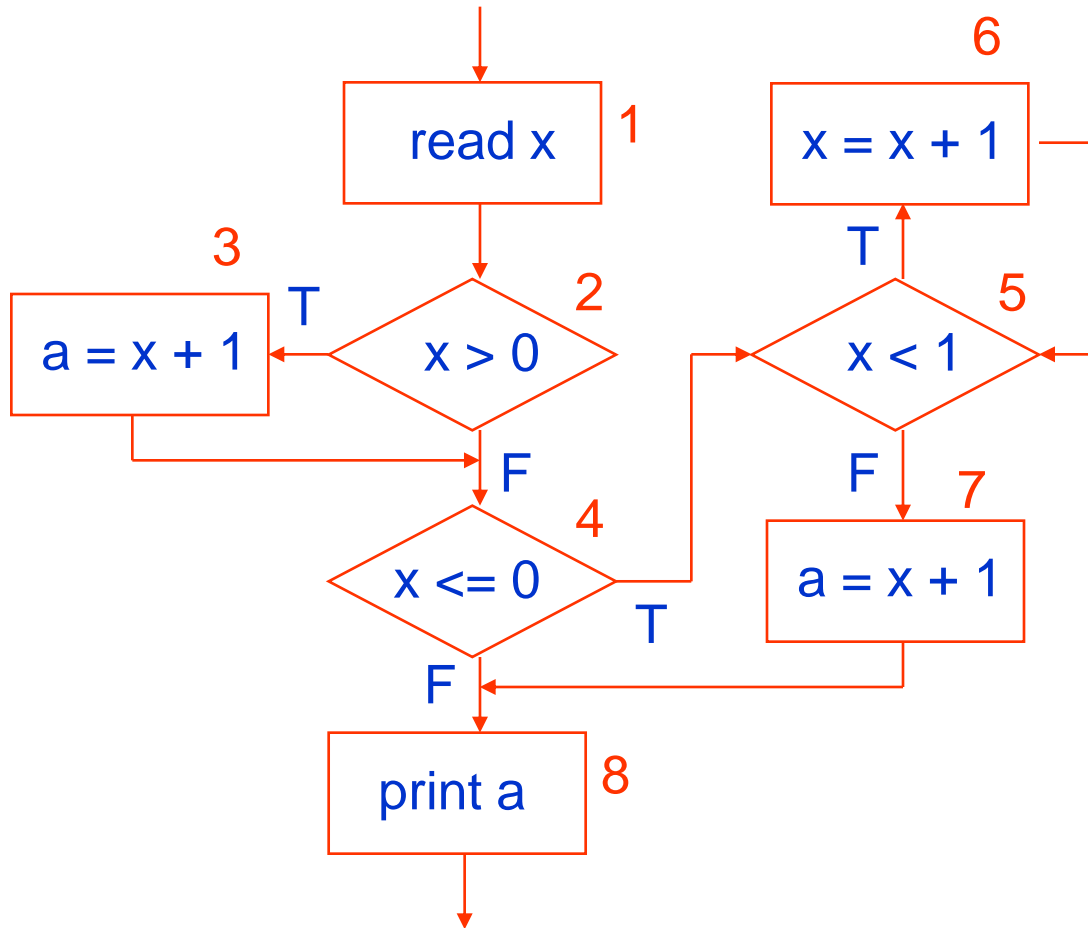
Slices

- A **slice** is a subset of a program.
 - When testing a program, most of the code in the program is **irrelevant** to what you are interested in. Slicing provides a convenient way of filtering out **irrelevant** code.
 - Slices can be computed automatically by statically analyzing the **control flow** and **data flow** of the program.
-

Slices

- A **slice** with respect to a **variable** v at a certain **point** p in the program is the **set of statements** that contributes to the value of the variable v at p .
 - We use $S(v, n)$ to denote the set of nodes in the control flow graph that contributes to the value of the variable v at node n .
-

An Example



$$S(x, 1) = \{1\}$$

$$S(x, 2) = \{1\}$$

$$S(x, 3) = \{1, 2\}$$

$$S(x, 4) = \{1, 2\}$$

$$S(x, 5) = \{1, 2, 4\}$$

$$S(x, 6) = \{1, 2, 4, 5, 6\}$$

$$S(x, 7) = \{1, 2, 4, 5, 6\}$$

$$S(a, 3) = \{1, 2, 3\}$$

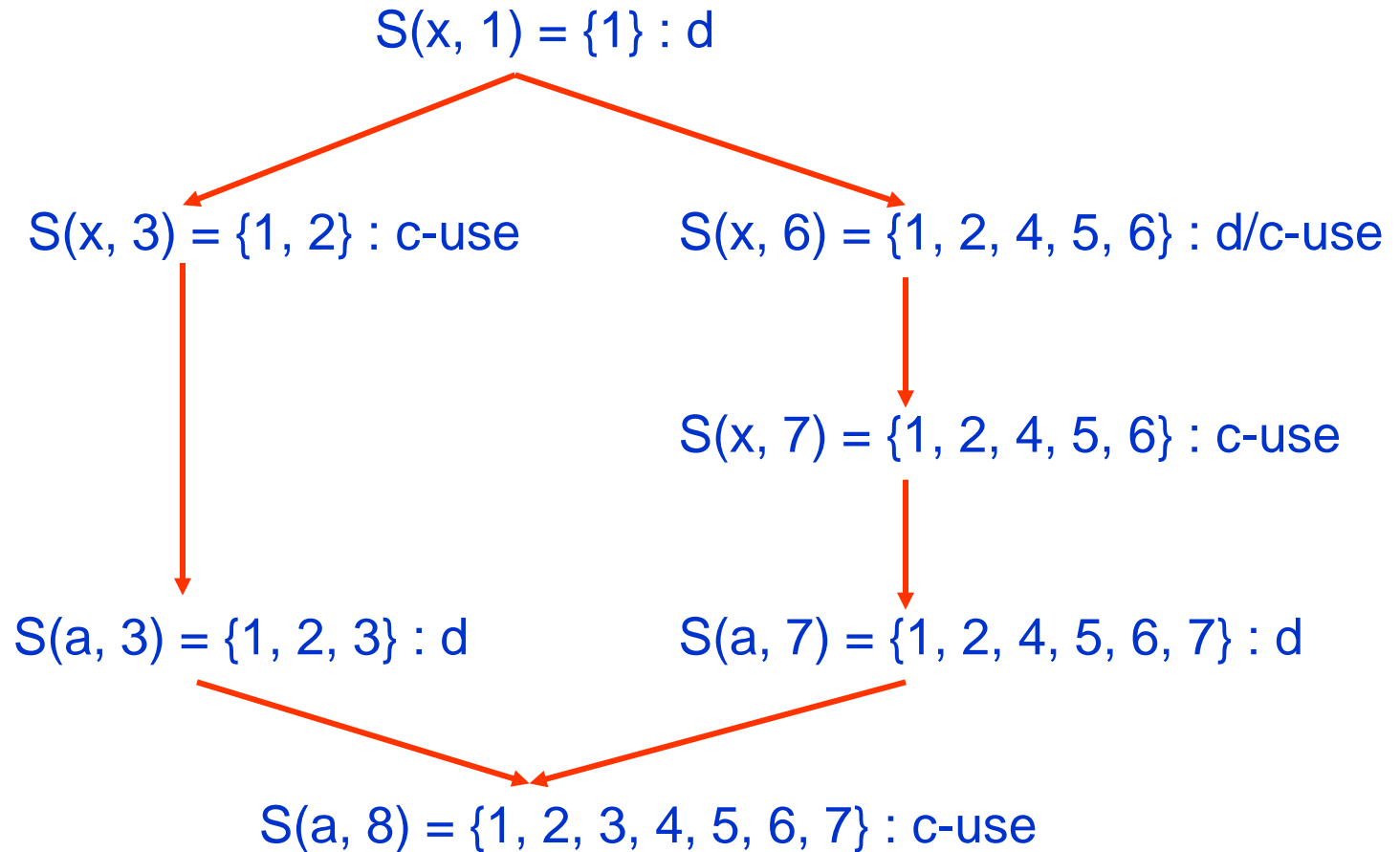
$$S(a, 7) = \{1, 2, 4, 5, 6, 7\}$$

$$S(a, 8) = \{1, 2, 3, 4, 5, 6, 7\}$$

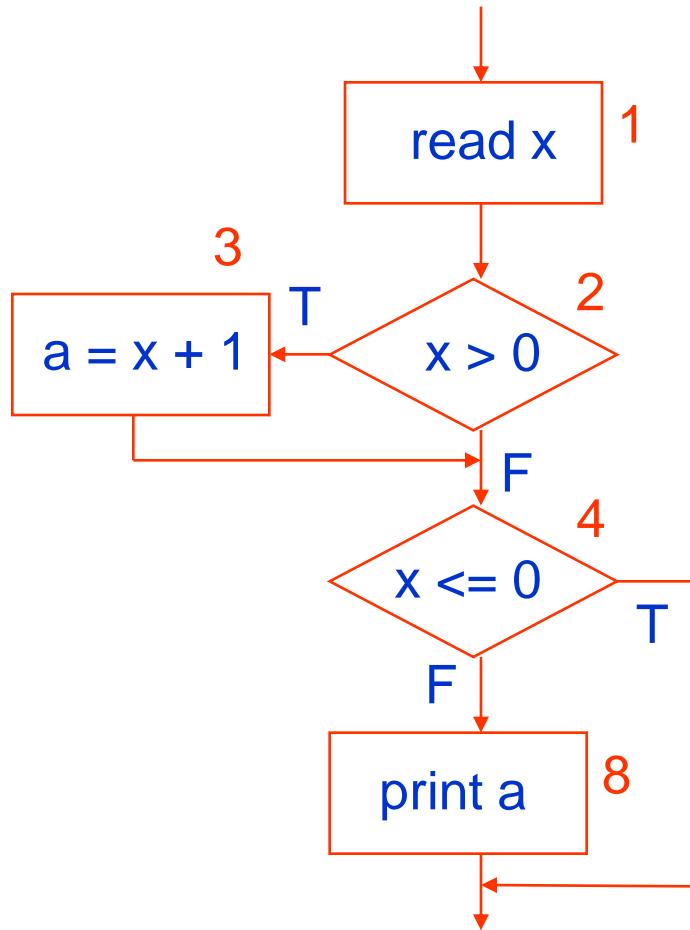
Lattices of Slices

- A definition of a variable v_n at node n usually uses the values of several variables v_1, \dots, v_m .
 - The slice $S(v_n, n)$ will contain the slices $S(v_1, n)$, \dots , $S(v_m, n)$.
 - These subset relationships induce a **lattice** on slices of different variables.
-

An Example



Test Case I



Test Case II

