## Assignment 1

## Regular Expressions and Finite Automata Due October 17, Wednesday, 2012

1. (30\%) Consider the following regular expression $(\varepsilon \mid a)^{*} \mid b^{+}$.
(a) $(15 \%)$ Give the expression tree for this regular expression. The precedence of operator ' + ' is the same as operator ' ${ }^{\prime *}$ '.
(b) ( $15 \%$ ) Give the set representation for the language at each node of the expression tree.
2. ( $20 \%$ ) Give a regular expression to define the following language: $\{a, a c, a b c, a b b c, a b b b c, a b b b b c, \ldots\}$.
3. $(50 \%)$ Consider the following nondeterministic finite automaton,

| States | a | b | $\varepsilon$ |
| :---: | :---: | :---: | :---: |
| 0 | $\{0,1\}$ |  |  |
| 1 |  | $\{2\}$ |  |
| 2 |  |  | $\{3,4\}$ |
| 3 | $\{3\}$ |  | $\{5\}$ |
| 4 | $\{6\}$ |  | $\{5\}$ |
| 5 | $\{7\}$ | $\{6\}$ |  |
| 6 |  |  |  |
| 7 |  |  |  |

where state 0 is the start state and state 7 is the only final state. The blank entry in the table represents the empty set.
(a) (30\%) Simulate this NFA using the $\varepsilon$-closure and move functions with respect to the input strings abaaaba and aabbbaa.
(b) (20\%) Give a regular expression for the language accepted by this NFA.

To turn in this assignment, upload a pdf file hw1.pdf that contains the solutions for this assignment to the eCourse site.

